OLCI Level 2
Algorithm Theoretical Basis Document

Rayleigh Correction Over Land
Document Signature Table

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1. INTRODUCTION

The Bottom of Rayleigh Reflectance (BRR) is a level 2 product over land that can be used in pixel classification. The Rayleigh correction formulation, defined for MERIS, remains pertinent for OCLI. One major improvement should be the use of a DEM of improved spatial resolution, and a smile correction is also simple to introduce.

The Rayleigh correction is based on the use of the Rayleigh atmospheric functions, which are computed as interpolated values within LUTs, and can be simplified, by using neural network approaches.

1.1 Acronyms and Abbreviations

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<td>BRR</td>
<td>Bottom of Rayleigh Reflectance</td>
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<tr>
<td>DEM</td>
<td>Digital Elevation Model</td>
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<td>MERIS</td>
<td>Medium Resolution Imaging Spectrometer</td>
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<td>MLP</td>
<td>Multilayers Perceptrons</td>
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<tr>
<td>OLCI</td>
<td>Ocean Land Colour Imager</td>
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<tr>
<td>ROT</td>
<td>Rayleigh Optical thickness</td>
</tr>
<tr>
<td>RTC</td>
<td>Radiative Transfer Code</td>
</tr>
<tr>
<td>SAA</td>
<td>Satellite Azimuth Angle</td>
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<td>SOS</td>
<td>Successive Order of Scattering code</td>
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<td>SZA</td>
<td>Sun Zenith Angle</td>
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<td>TOA</td>
<td>Top of Atmosphere</td>
</tr>
<tr>
<td>VAA</td>
<td>Viewing Azimuth Angle</td>
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<td>VZA</td>
<td>Viewing Zenith Angle</td>
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1.2 Purpose and Scope

BRR can be used to produce land classification maps to start an algorithm for aerosol remote sensing... Therefore an implementation in OCLI is adopted. Using the simple procedure in Section 2, we can determine the BRR from the top of atmosphere (TOA) reflectance. The definition and the basic way to compute the Rayleigh function is described in Section 3. What is done for MERIS is applicable to OCLI Section 4, but improvements can be conducted as indicated in Section 5.

1.3 Algorithm Identification

This algorithm is identified under reference “SD-03-C15” in the Sentinel-3 OLCI documentation.

2. ALGORITHM OVERVIEW

2.1 Theoretical Description

A Simplified formulation of the Rayleigh contribution

Outside of the strong absorption bands (i.e., in the O$_2$ and H$_2$O bands), the coupling between scattering and gaseous absorption remains relatively weak. This assumption leads to express the apparent reflectance $\rho^*$ at top of the atmosphere (TOA) as:

$$\rho^* = \rho_{na}^* \cdot T_g$$  \hspace{1cm} (1)

Where $\rho_{na}^*$ is the signal ignoring the gaseous absorption and $T_g$ the gaseous transmittance. The next step is to correct for the well known Rayleigh scattering. To do so, a simplified formulation of the signal will be used followed by an indication of how the different Rayleigh scattering functions were computed. Then, we will illustrate the limitations of this Rayleigh correction.
A simple two-layer model shows a schematic representation of the atmosphere: molecules over aerosols. The spectral dependency of the Rayleigh optical thickness is well known. This optical thickness is proportional to the barometric pressure \( P \) at the ground surface. The geometry of the observation is described by the solar and viewing zenithal angles, respectively \( \varphi_s \) and \( \varphi_v \) (or the cosine of this zenith angle \( \mu \)), and by the difference in azimuth \( \varphi \). Thus, the Rayleigh contribution above the aerosol-ground system can be written, following the 6S code formulation, Vermote et al. (1997), as:

\[
\rho_{na}^* = \rho_R + T_R(\mu_s) \cdot \frac{\rho_{aG}}{1 - \rho_{aG} \cdot S_R} \cdot T_R(\mu_s) 
\]

where \( \rho_{na}^* \) is the apparent reflectance at TOA (corrected for gaseous absorption), \( \rho_R \) the Rayleigh reflectance, \( \rho_{aG} \) the aerosol-ground system reflectance, \( T_R(\mu_s) \) and \( T_R(\mu_v) \) the downward and upward Rayleigh transmittance respectively and \( S_R \) the spherical albedo relating to the molecules.

There are two basic assumptions contained in equation (2):

(i) On the vertical distribution: the molecular layer is put above the aerosol layer.

(ii) On the bi directionality of the radiances at the top of the aerosol layer. The BRR (bottom of Rayleigh) is assumed to be Lambertian.

According to Equation 2, we can easily correct for Rayleigh scattering to retrieve the reflectance above the aerosol-ground system. First, if we ignore the coupling between reflection and scattering:

\[
\rho_{aG}^C = (\rho_{na}^* - \rho_R) / T_R(\mu_s) \cdot T_R(\mu_v) 
\]

Second, after correction of this term:

\[
\rho_{aG} = \frac{\rho_{aG}^C}{1 + \rho_{aG}^C \cdot S_R} 
\]
**Definition and computation of the Rayleigh scattering functions**

**Standard values of the Rayleigh optical thicknesses**

The Rayleigh optical thickness, ROT, \( \tau_R(\lambda, R) \) is estimated for each OCLI band \( j \) \( (Hansen and Travis, 1974) \); \( \lambda \) is the nominal central wavelength and the pressure \( P_{\text{std}} \) is the standard pressure (1012 hPa).

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<th>412.50</th>
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*Table 1*: Rayleigh optical thickness in 13 MERIS spectral bands.

**The Fourier series expansion of the radiation field**

Most of the radiative transfer codes (RTC) use a Fourier series expansion of the radiation field as:

\[
\tilde{L}_R(\theta_s, \theta_v, \Delta \phi) = \sum_{s=0}^{2} (2-\delta_{0,s}) \tilde{L}_s^R(\theta_s, \theta_v) \cos(s \Delta \phi)
\]

(5)

For the Rayleigh scattering, the Stokes vector \( \tilde{L}_R \) is expanded in three Fourier terms \( \tilde{L}_s^R \) (s=0,1,2). \( \theta_s, \theta_v, \Delta \phi \) are respectively the solar zenith angle, the view zenith angle, the difference in azimuth; \( \delta_{0,s} \) is the Dirac's function.
Rayleigh primary scattering

In the near infrared, the primary scattering regime dominates. The incident solar light is unpolarized. For the primary scattering, the Stoke vector is reduced to the radiance, or to the reflectance. At TOA, we express the Rayleigh reflectance for the 3 Fourier series terms as the product of the Rayleigh phase function by a term depending on the geometry and on the ROT.

\[ \rho_{R,p}^{(s)}(\vartheta_s, \vartheta_r, e^R) = P_R^{(s)}(\vartheta_s, \vartheta_r) \cdot \frac{(1 - e^{-M \cdot e^R})}{4 \cdot (\cos \vartheta_s + \cos \vartheta_r)} \]  

(6)

with, \( M \), the air mass defined as:

\[ M = \frac{1}{\cos \vartheta_s} + \frac{1}{\cos \vartheta_r} \]  

(7)

The Fourier series expansion of the Rayleigh phase function

\( P_R^{(s)} \) the Rayleigh phase function for each Fourier series term \( s \) is independent on the wavelength and expressed as:

\[
\begin{align*}
    P_R^{(0)}(\vartheta_s, \vartheta_r) &= \frac{3A}{4} \left( 1 + \cos^2 \vartheta_s \cdot \cos^2 \vartheta_r + \frac{\sin^2 \vartheta_s \cdot \sin^2 \vartheta_r}{2} \right) + B \\
    P_R^{(1)}(\vartheta_s, \vartheta_r) &= -\frac{3A}{8} \cdot \cos \vartheta_s \cdot \cos \vartheta_r \cdot \sin \vartheta_s \cdot \sin \vartheta_r \\
    P_R^{(2)}(\vartheta_s, \vartheta_r) &= \frac{3A}{16} \cdot \sin^2 \vartheta_s \cdot \sin^2 \vartheta_r
\end{align*}
\]  

(8)

with \( A = 0.9587256 \), \( B = 1 - A \)

A and \( B \) are the coefficients which account for the molecular asymmetry

The successive order of scattering and the Rayleigh reflectance

The Rayleigh scattering is computed using the successive order of scattering code (SOS), *Deuzé et al. (1989)*. The code solves the radiative transfer equation in the vector mode.
Simulations underline the need to account for the polarization in the Rayleigh reflectance computations (Santer et al., 2002). If not, relative errors as high as 6 percent can be made.

We introduce a multiplicative function $f_R^{(s)}$ which accounts for the multiple scattering. Thus the Rayleigh reflectance $\rho_R^{(s)}$ for each Fourier series term $s$ is written as:

$$\rho_R^{(s)}(\vartheta_s, \vartheta_v, \tau^R) = \rho_{R,p}^{(s)}(\vartheta_s, \vartheta_v, \tau^R) \cdot f_R^{(s)}(\vartheta_s, \vartheta_v, \tau^R)$$

(9)

where $\rho_{R,p}^{(s)}$, the primary scattering reflectance for Rayleigh.

What are the advantages of these different decompositions:

(i) The Fourier series expansion has only 3 terms.

(ii) The primary scattering has a simple analytical formulation.

(iii) The multiplicative function $f_R^{(s)}$ can be fitted by a polynomial of order 2.

The Rayleigh transmittances

The Rayleigh transmittance applies both on the downward and upward paths. Following the principle of reciprocity, it is the same function depending only on the zenith angle.

A quite accurate formulation is available in the 6S code (Vermote et al., 1997):

$$T_R^{6S}(\tau_R, \mu) = \frac{(2/3+\mu) + (2/3-\mu)e^{-\tau_R/\mu}}{(4/3+\tau_R)}$$

(10)

The transmittance is defined as the ratio between the downwelling total irradiance (direct + diffuse) at the surface to the incident solar irradiance at TOA. In the SOS code, the solar irradiance at TOA is normalized to $\pi$.

$$T_R^{SOS}(\tau_R, \mu) = \exp(-\tau_R/\mu) + \phi^R(\mu, \tau_R)$$

(11)

The computation of the diffuse irradiance $\phi^R(\mu, \tau_R)$ requires only the Fourier series term $s=0$ with:
\[ \phi^R_k(\mu, \tau_R) = 2\pi \int_0^1 L^R_{\mu} (\tau_R, \mu, \mu) \, d\mu \]  

(12)

In the SOS code, the angular integration is made with 24*2 Gaussian angles (±2 for up and down). The Gaussian quadrature is applied to Eq. (12):

\[ \phi^R_k(\mu, \tau_R) = 2\pi \sum_{j=1}^{24} I_{\mu}^0(\mu, \mu_j, \tau_R) w_j \]  

(13)

\( \mu_j \) and \( w_j \) are respectively the cosine and the weight of the 24 Gaussian angles.

**The Rayleigh spherical albedo**

The *Rayleigh* spherical albedo \( S_R \) is defined as

\[ S_R(\tau_R) = 1 - 2 \int_0^1 T_R(\tau_R, \mu) \mu \, d\mu \]  

(14)

Using the Gaussian quadrature:

(i) \( T_R(\mu, \tau_R) \) is computed with the SOS code for 24 Gaussian angles as solar zenith angle and \( s=0 \).

(ii) Using the Gaussian quadrature, Eq. (14) is rewritten as:

\[ S_R(\tau_R) = 1 - 2 \sum_{j=1}^{24} T_R(\tau_R, \mu_j) w_j \]  

(15)

**2.2 MERIS like computation and associated LUTs**

**Grid for Rayleigh computation**

The Rayleigh scattering functions are computed at the centre of a 4*4 pixels grid in which we know the:
(i) geometrical conditions: SZA, VZA, SAA, VAA.
(ii) sea level pressure $P_o$.
(iii) The surface elevation $z$.

Rayleigh phase function computation

We first compute the scattering angle $\Theta$. The Rayleigh phase function is expressed as:

$$ P_R(\Theta) = 3A(1+\cos^2(\Theta))/4+B $$

with $A = 0.9587256$, $B = 1-A$ (16)

Rayleigh optical thickness computation

The ROT $\tau_R^j$ for the 13 MERIS nominal bands $j$ are in a LUTs. They are corrected by the barometric pressure at the surface elevation with:

$$ P(z) = P_o \exp(-z/8000) $$

(17)

according to the molecular scale height of 8 000 m, if $z$ is in metres.

Eq. (17) is an approximation which needs to be revisited. The temperature at surface level is an additional parameter to $z$ to trigger the altitude correction from the sea level pressure to the surface pressure.

For the window, the ROT are weighted by the pressure with:

$$ \tau_R^j(P_o,z) = P(z)\tau_R^j/P_{\text{atd}} $$

(18)

Rayleigh primary scattering computation

The reflectance is computed following:

$$ \rho_{k,p}^j = P_R(\Theta) \frac{(1-\exp(-M\tau_R^j))}{4(\cos\theta + \cos\theta')} $$

(19)
The wavelength dependence is contained in $\tau_k^j$.

**Rayleigh reflectance computation**

The multiplicative Rayleigh scattering functions $f_R^{(s)}$, determined for each of the first 3 Fourier series terms $(s)$, have been expanded as:

$$f_R^{(s)}(\vartheta,\varphi,\tau_R) = \sum_{i=0}^{3} k_i^{(s)}(\vartheta,\varphi)(\tau_R)^i \quad (20)$$

with $k_i^{(s)}$ the polynomial coefficients for the Fourier series term $s$. $k_i^{(s)}$ are pre-computed in LUT for $s=0,1,2$ and 12 Gaussian angles. A double linear interpolation (in SZA and VZA) to produce $k_i^{(s)}(\theta,\varphi)$.

In a loop on the 13 MERIS bands, we then compute $f_R^{(s)}(\vartheta,\varphi,\tau_k^j)$. The Rayleigh scattering function ($f_R^j$) will be then computed by recombining the first 3 Fourier series terms as follows:

$$f_R^j(\vartheta,\varphi,\Delta \varphi) = \sum_{s=0}^{3} (2-s) f_R^{(s)}(\vartheta,\varphi,\tau_k^j) \cos(s \Delta \varphi) \quad (21)$$

Finally, the Rayleigh reflectance is:

$$\rho_k^j = f_R^j(\vartheta,\varphi,\Delta \varphi) \rho_{k,P}^j \quad (22)$$

**Rayleigh transmittance computation**

For the 13 MERIS bands, the Rayleigh transmittance ($T_R$) is estimated with a second order polynomial function of the Rayleigh transmittance derived from the 6S model ($T_R^{6S}$), see Eq. (10):
\[ T_R(\tau_R, \mu_s) = \sum_{i=0}^{2} t_i (T_R^{SS}(\tau_R, \mu_s)) \]  

(23)

Where \( \mu_s \) is the cosine of solar zenith angle \( (\theta_s) \) and \( \tau^R \) is the Rayleigh optical thickness. The \( t_i \) polynomial coefficients (LUT074). This computation applies as well to the upward path (\( \mu_u \) instead of \( \mu_s \)).

**Rayleigh spherical albedo computation**

Eq. (15) is used to generate the spherical albedo with ROT between 0.02 and 0.32 with a step of 0.02. The details on the MERIS computations are available from the MERIS Level-2 detailed processing model (*MERIS L2 DPM, 2005*).

**The LUTs**

The details on the MERIS LUTs are available in (*Zagolski et al, 2005*) and the Rayleigh LUTs are described in Table 2.

Table 1 is LUT097. The other LUTs have been generated with the SOS code using the 24 Gaussian angles of LUT080. To save space and time, a subset of 12 Gaussian angles has been selected (2.84, 17.63841, 28.76843, 36.18973, 43.61145, 51.03339, 58.45547, 65.87766, 69.58877, 73.29988, 77.01101 and 80.72215). With the symmetry \( (\theta_s, \theta_u) \), the scattering coefficients \( f \) (LUT101) are produced for 78 pairs of zenith angles (LUT081).

The three transmittance coefficients have been produced from the computation by the SOS code of \( T_R^{SOS}(\tau_R, \mu=1) \) for a sun at zenith and 17 ROTs. The limitation at \( \theta_s = 0^\circ \) needs to be evaluated. The larger value of the ROT is 0.32 with corresponds to 412 nm. The selection for OCLI of a band at 400 nm will impose to add two values (0.34 and 0.36). The smaller value of the ROT is 0.02, which means that B13 and B14 are already extrapolated. It certainly relevant to add ROT=0 in the LUTs. It will give:

(i) verify (or impose) \( k_0^{(i)} = 0 \)

(ii) verify (or impose) \( t_0 = 0 \)

(iii) impose \( S_R(\tau_R=0)=0 \)
Table 2: The Rayleigh LUTs

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<td>LUT080</td>
<td>$\Theta$</td>
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<td>78</td>
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<td>$3 \times 78 \times 3$</td>
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<tr>
<td>LUT074</td>
<td>transmittance coefficient</td>
<td>$t_0, t_1, t_2$</td>
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<td>LUT102</td>
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2.3 Algorithm Validation

To be completed in a future issue of this document.

3. ASSUMPTIONS AND LIMITATIONS

The Baseline is the MERIS-like algorithm, with a better DEM, in order to keep it out of the critical path. Alternatively, the O2 surface pressure can be used to replace the ECMWF pressure combined with the DEM improvement. An future evolution is the use of Neural Networks to replace the interpolations made on the grid points of the LUTs.

3.1 Limitation of the MERIS like approach and recommendations for OCLI
The smile effect

It is possible to simply include the smile correction with:

\[ \tau_R^{(i)}(P_o, z, \lambda) = \tau_R^{(i)}(P_o, z)(\lambda_j/\lambda)^4 \]  \hspace{1cm} (24)

is the nominal wavelength for band j, \( \lambda_j \) is the effective wavelength for band j and for pixel i. For MERIS, the amplitude of the smile is 1 nm. In the blue, the smile effect impacts the ROT by one percent. It is small but when it is possible to correct it …

Resolution of the DEM

In BEAM, it is possible to use a DEM with a resolution of 1 km (getasse option). Using Eq. (7), we compute the pressure with the MERIS DEM and this high resolution DEM. We illustrate in Figure 1 the two possibilities. Clearly, over mountains, the current MERIS DEM does not offer the required surface pressure.
A better DEM is required and key information can be derived as well from a high resolution DEM as soon as the geo localisation is satisfactory. The terrain slope is an indicator on the validity of the conversion of radiance to reflectance. This conversion assumes the surface to be horizontal in mean in the pixel. The dream is to have an accurate surface pressure derived from the oxygen band(s?) in the Rayleigh computation.

**Use of the O₂ derived surface pressure**

MERIS has two spectral bands (B10 and B11) to derive over land the surface pressure. At the very beginning, this O₂ surface pressure was planned to be used in two ways:

(i) In the pixel classification to detect the presence of semi transparent clouds such as cirrus clouds.
(ii) To compute the Rayleigh optical thickness.

The poor quality of the surface pressure product resulted in the de-scoping of its involvement in the two tasks. Through the ongoing O$_2$ project, substantial improvements have been made on this MERIS O$_2$ surface pressure. For OLCI, we will have an additional spectral band in the O$_2$ absorption lines and therefore we can expect to even have a better determination.

Replace the LUTs by a neural network.

A good way to approximate the radiative transfer is to use artificial neural networks (ANN). A particular class of ANN, the so-called multilayers perceptrons (MLP), was used by Brajard et al, 2009, to simulate the atmospheric reflectance transmittance in the MERIS bands over water. One MLP is dedicated to the simulation of $\rho_{\text{atm}}$ (denoted MLP-A), and one to $T$ (MLP-T). A sub-dataset of 150 000 $\rho_{\text{atm}}$ (resp. $T$) was randomly extracted from LUT-A (resp. LUT-T) to calibrate MLP-A (resp. MLP-T). Figure 2 is a representation of the MLP.

![Figure 2: Representation of the two MLPs used to simulate the direct model.](image)

This approach is simplified for the Rayleigh. Only $(\theta_s)$, $(\theta_v)$, $(d\phi)$ and $(\tau_R)$ are the inputs for the MLP for the reflectance. Only $(\theta_s)$, $(\Omega)$ and $(\tau_R)$ are the inputs for the MLP for the
transmittance. It will be faster and more accurate than the previous approach, and also simpler to code it.

4. INPUT DATA

Geometry including illumination and viewing zenith and azimuth angles: $\theta_s$ [degrees], $\theta_v$ [degrees] and $d\phi$ [degrees]

Apparent reflectance at TOA (corrected for gaseous absorption): $\rho_{na}^*$ [dimensionless]

DEM: Digital Elevation Model [m] from external source

5. ERROR BUDGET

Assuming that:

(i) the smile effect is corrected

(ii) the good accuracy of the DEM and it good spatial

The key input is the barometric pressure and the error impact can be simply evaluated from the 6S formulation, see equation 3. To some extent, because the production of the land surface reflectance does not account for aerosols, an error budget is of lower importance.

In order to give an idea on the error, we compute the TOA signal for a pure molecular atmosphere, a nadir view and a solar angle of 60 degrees for three surface albedos: 0.15, 0.3 and 0.5. The signal was computed for a pressure of 1007 hPa and inverted with 1012 hPa. The results are reported in absolute error on albedo (in percentage) on figure 3.
If we want to estimate the error, the simple way to implement the error bar is to do two Rayleigh corrections: one with the nominal pressure and the second by adding an error on it (nominal is 5 hPa). Alternatively, we can to the first order compute the correction based on the Rayleigh functions:

The Rayleigh computation of the optical thickness $\tau_R^0$, of the reflectance $\rho_R^0$ and of the transmittances total $T_R^0$ are conducted for the ECMWF surface pressure $P_0$ and we used a pressure $P = P_0 + dP$ to evaluate the error. We directly have:

$$d \tau_R = \tau_R^0 \frac{dP}{P_0} \quad (25)$$

$$d \rho_R = \rho_R^0 \frac{dP}{P_0} \quad (26)$$

$$T_R = T_R^0 \exp(-0.5 \frac{d \tau_R}{\mu}) \quad (27)$$

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Figure 3: Absolute error on the retrieval of the Bottom of Rayleigh Reflectance (in percent) versus the wavelength for 3 “white” values of the surface albedo. Error on the barometric pressure is 5 hPa.
And with these corrected Rayleigh functions, we use again Eq. (3) to get a second value of the surface reflectance to determine the error bar.

6. REFERENCES


